The final word on undulators, FELs & compact sources, x-ray detectors.

• Undulator coherence

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- Emittance

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$$\sum_{m=0}^{N-1} e^{i(\vec{k}\cdot\vec{r}+2\pi m\epsilon)} = e^{i\vec{k}\cdot\vec{r}} \sum_{m=0}^{N-1} e^{i2\pi m\epsilon}$$

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$$S_N - kS_N = 1 - k^N \quad \longrightarrow \quad S_N = \frac{1 - k^N}{1 - k}$$

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Therefore, for the diffraction grating we can calculate the intensity at the detector as

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$$I = \frac{\sin(\pi N\epsilon)^2}{\sin(\pi\epsilon)^2}$$

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Beam Coherence

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With the height and width of the peak dependent on the number of poles.

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Undulator Coherence



Undulator Coherence



APS Parameters

Table 1: APS SR Beam Stability Requirement Evolution

Parameter	Units	RMS Beam Size and <i>stability requirement</i>		
		(5 % of beam dimensions) at IDs in year		
		1995	2001	2005
$\sigma_{\rm x}$	μm	334	352	280
x		16.7	17.6	14
$\sigma_{x'}$	μrad	24	22	11.6
<i>x</i> '		1.2	1.1	0.58
$\sigma_{\rm v}$	μm	89	18.4	9.1
y		4.45	0.92	0.45
$\sigma_{v'}$	μrad	8.9	4.2	3.0
<i>y</i> ['] ,		0.45	0.21	0.15
Eeff	nm-	8	77	3.2
- 611	rad	0	1.1	5.2
Coupling	%	10.0	1.0	0.9

For photon emission from a single electron in a 2m undulator at 1Å $\sigma_{\gamma} = \frac{\sqrt{L\lambda}}{4\pi} = 1.3 \mu m \qquad \qquad \sigma_{\gamma}' = \sqrt{\frac{\lambda}{L}} = 7.1 \mu rad$

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must convolute to get photon emission from entire beam (in vertical direction)

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$$\sigma_{radiation} = 9.1 \mu m$$

$$\sigma'_{\it radiation}=7.7\mu {\it rad}$$

Synchrotron Time Structure



9 / 20





• Initial electron cloud, each electron emits coherently but independently



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- Over course of 100 m, electric field of photons, feeds back on electron bunch



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- Over course of 100 m, electric field of photons, feeds back on electron bunch
- Microbunches form with period of FEL (and radiation in electron frame)
- Each microbunch emits coherently with neighboring ones

FEL Emission



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FEL Layout



Compact Sources



Gas detectors

Gas detectors

Scintillation counters

Gas detectors

Scintillation counters Solid state detectors

Gas detectors

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Gas detectors

Ionization chamber

Scintillation counters Solid state detectors

Gas detectors

- Ionization chamber
- Proportional counter

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Scintillation counters Solid state detectors

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- P-I-N junction

Charge coupled device detectors

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Scintillation counters Solid state detectors

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Charge coupled device detectors

- Indirect
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Gas Detector Curve





Useful for beam monitoring, flux measurement, fluorescence measurement, spectroscopy.



• Closed (or sealed) chamber of length L with gas mixture $\mu = \sum \rho_i \mu_i$



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- Count rates up to 10¹¹ photons/s/cm³
- 22-41 eV per electron-hole pair (depending on the gas) makes this useful for quantitative measurements.

Useful for photon counting experiments



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- Photoelectrons are accelerated in steps, striking dynodes and becoming amplified.
- Output voltage pulse is proportional to initial x-ray energy.

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Solid State Detectors

Open circuit p-n junction has a natural depletion region



depletion region

Solid State Detectors

Open circuit p-n junction has a natural depletion region



When reverse biased, the depletion region grows

Solid State Detectors

Open circuit p-n junction has a natural depletion region



When reverse biased, the depletion region grows creating a higher electric field near the junction

Ge Detector Operation



Silicon Drift Detector

Same principle as intrinsic or p-i-n detector but much more compact and operates at higher temperatures



Relatively low stopping power is a drawback

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